

# Surface energy coefficient of a low density nuclear system

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Since the earliest observations of nuclear multifragmentation (the break up of excited nuclei), the Fisher Droplet Model (FDM) [1] has been employed in attempts to understand this phenomenon. It still enjoys great popularity and has been employed in the analysis of the EOS Au multifragmentation data [2]-[4].

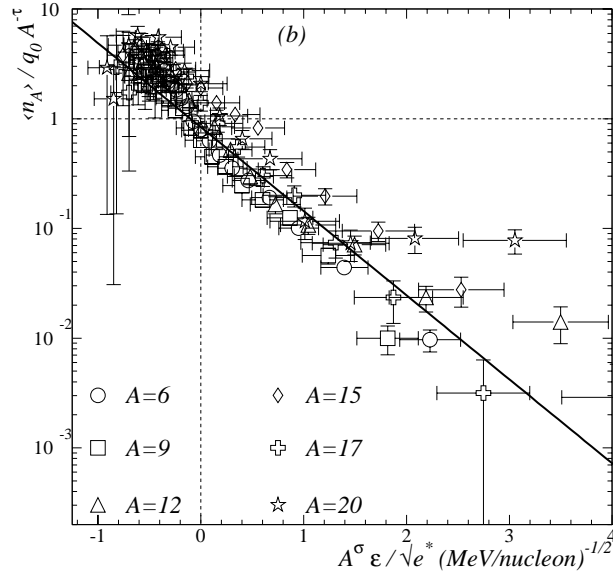


Figure 1: Scaled fragment distribution as a function of the scaled control parameter for fragments of mass  $A$ ; solid line: a fit to the FDM.

The FDM is based on the equilibrium description of droplets. The mean number of droplets of size  $A$  is written as:

$$\langle n_A \rangle = \left\langle \frac{N_A}{A_0} \right\rangle = q_0 A^{-\tau} \exp \left[ \frac{A \Delta \mu}{T} - \frac{c_0 \epsilon A^\sigma}{T} \right],$$

where:  $\Delta \mu = \mu - \mu_l$ ;  $\mu$  and  $\mu_l$  are the actual and liquid chemical potentials respectively;  $A_0$  is the size of the system;  $q_0$  is a normalization constant depending only on the value of  $\tau$ ;  $\tau$  depends on the dimensionality of the system;  $c_0 \epsilon A^\sigma$  is the surface free energy of a droplet;  $c_0$  is the surface

energy coefficient;  $\sigma$  is the critical exponent related to the ratio of the dimensionality of the surface to that of the volume; and  $\epsilon = (T_c - T)/T_c$  is the control parameter, a measure of the distance from the critical point,  $T_c$ .

Fig. 1 shows a plot of the EOS Au multifragmentation data [2]-[4]. The substitution of  $\sqrt{e^*} = \sqrt{E^*/A_0}$  for  $T$  has been made resulting in a control parameter of  $\epsilon = (\sqrt{e_c^*} - \sqrt{e^*})/\sqrt{e_c^*}$ ; for a degenerate Fermi gas reduces to  $(T_c - T)/T_c$ . The excitation energy normalized to the mass of the fragmenting remnant,  $e^*$  in MeV/nucleon, excludes collective effects [3]. The location of the critical point,  $e_c^*$ , and values of the critical exponents,  $\sigma$  and  $\tau$ , were determined previously [2]-[4]. Fitting  $n_A^{scaled}$  as a function of  $\epsilon^{scaled}$  for  $\epsilon \geq 0$  and leaving  $c_0$  and  $\exp[A \Delta \mu / \sqrt{e^*}]$  as free parameters in the FDM gives  $c_0 = 6.4 \pm 0.6$  MeV (via  $E^* = aT^2$  with  $a = A_0/13$ ) and  $\exp[A \Delta \mu / \sqrt{e^*}] = 0.8 \pm 0.1$ , *i.e.* the bulk term is consistent with  $\Delta \mu \approx 0$ . The temperature independent surface energy coefficient  $c_0$  is of a different nature than the semiempirical mass formula parameter ( $a_s \sim 17$  MeV for  $T = 0$ ,  $\rho = \rho_0$ ) or estimates for low density nuclear systems ( $a_s \sim 6$  MeV for  $T \sim 3$  MeV,  $\rho \sim \rho_0/3$ ) [5].

## References

- [1] M. E. Fisher, *Physics* **3**, 255 (1967).
- [2] M. L. Gilkes, *et al.*, *Phys. Rev. Lett.* **73**, 1590 (1994).
- [3] J. A. Hauger *et al.*, *Phys. Rev. C* **57**, 764 (1998).
- [4] J. B. Elliott *et al.*, *Phys. Lett. B.* **418**, 35 (1998).
- [5] A. S. Hirsch *et al.*, *Phys. Rev. C* **29**, 508 (1984).